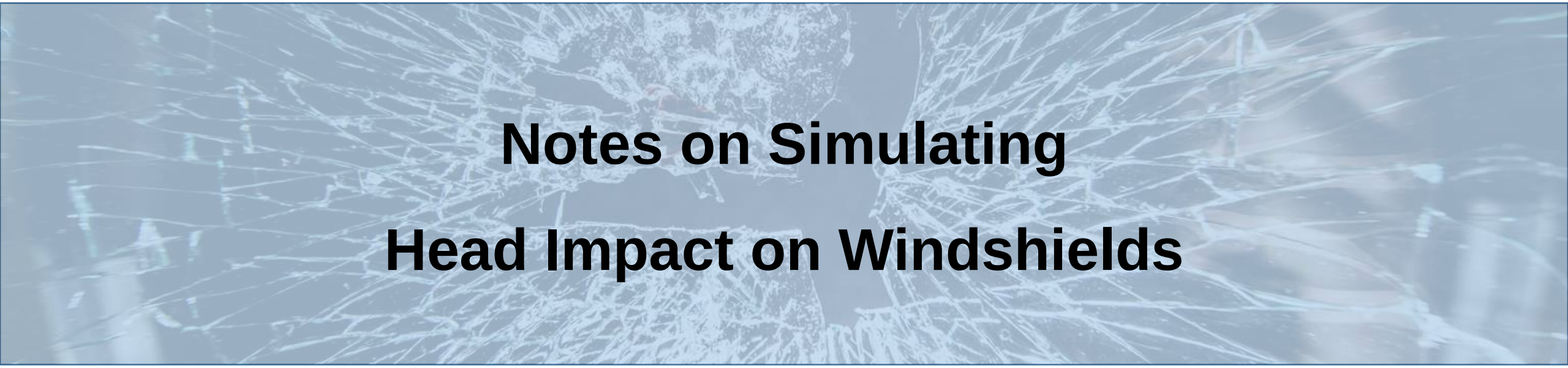


Notes on Simulating Head Impact on Windshields

Stefan Kolling, Christopher Brokmann, Christian Alter

Introduction and Content



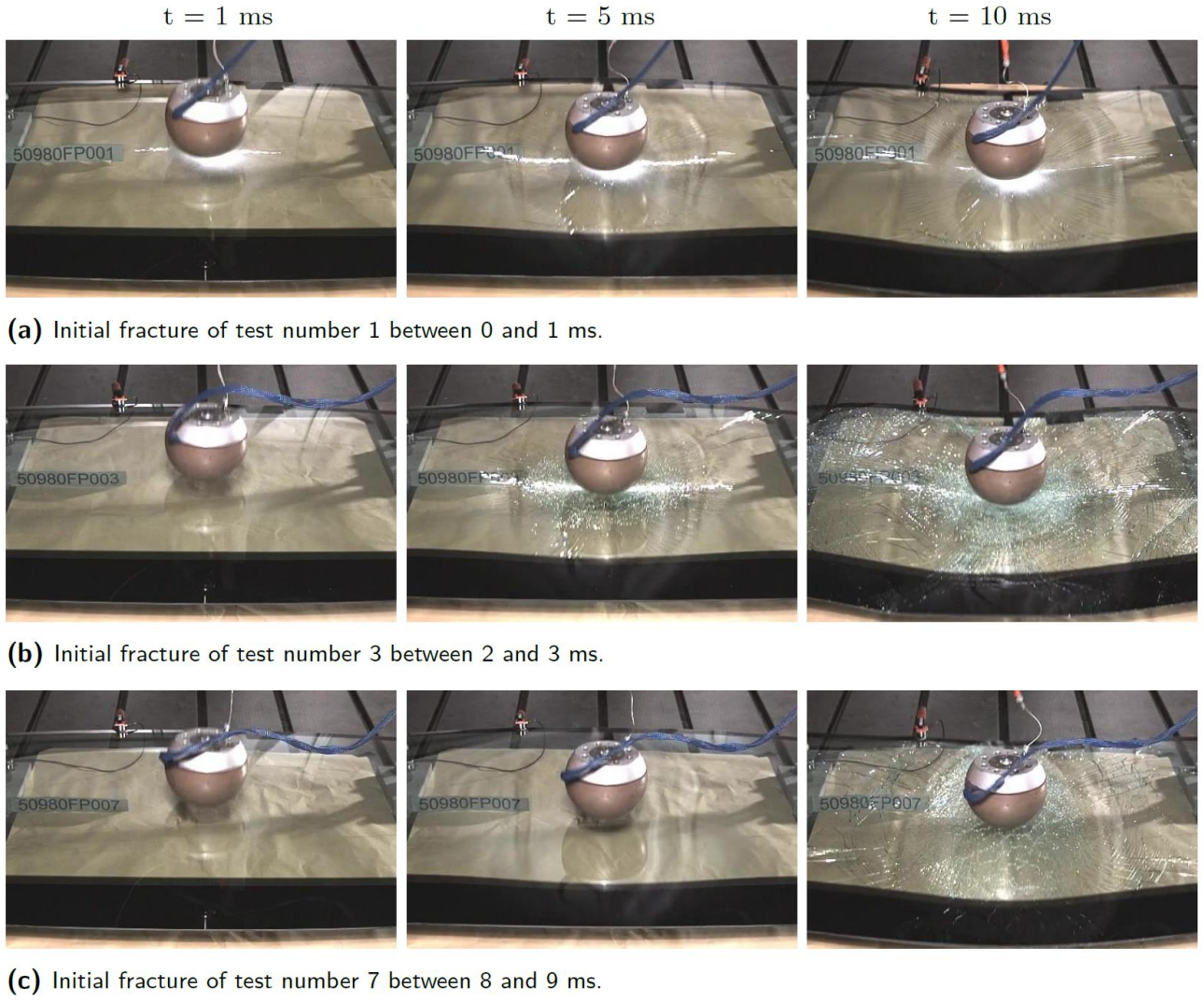
Source: hondanews.com

- Reproducibility of head impact tests on windshields
- Probability of glass fracture
- FE-modelling of laminated glass
- Stochastic simulation

Source: BGS Böhme & Gehring GmbH

Motivation: How Reproducible are Head Impact Tests?

- Audi A3 windshields
- Free-flying head
- 10 m/s, centric, 10 tests
- Euro NCAP adult head
- Four-point support



(a) Initial fracture of test number 1 between 0 and 1 ms.

(b) Initial fracture of test number 3 between 2 and 3 ms.

(c) Initial fracture of test number 7 between 8 and 9 ms.

Motivation: How Reproducible are Head Impact Tests?

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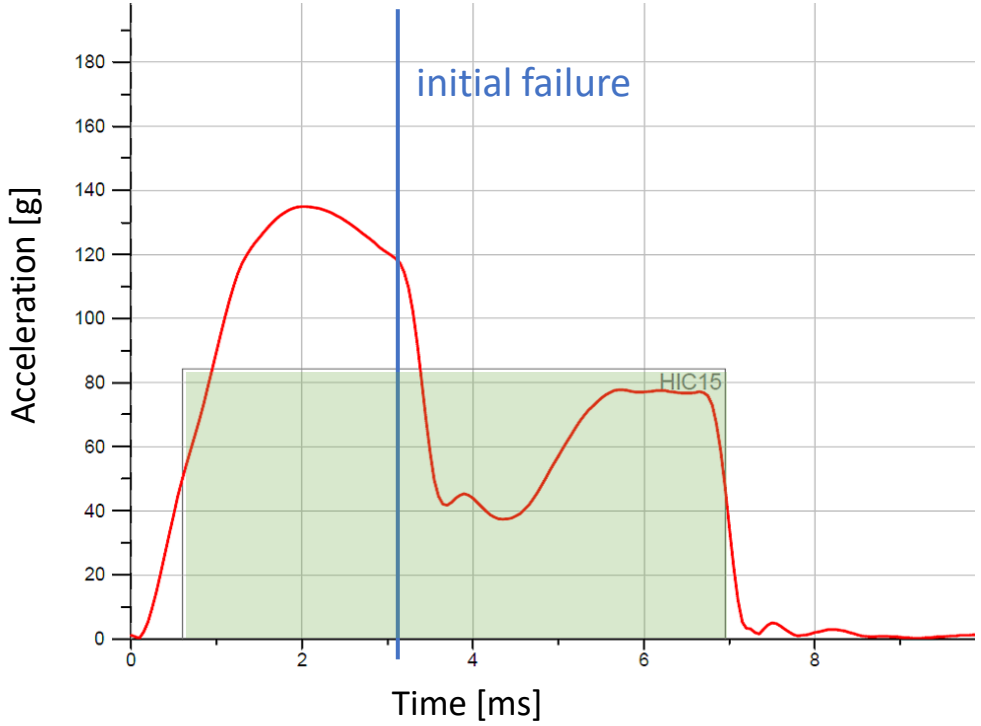
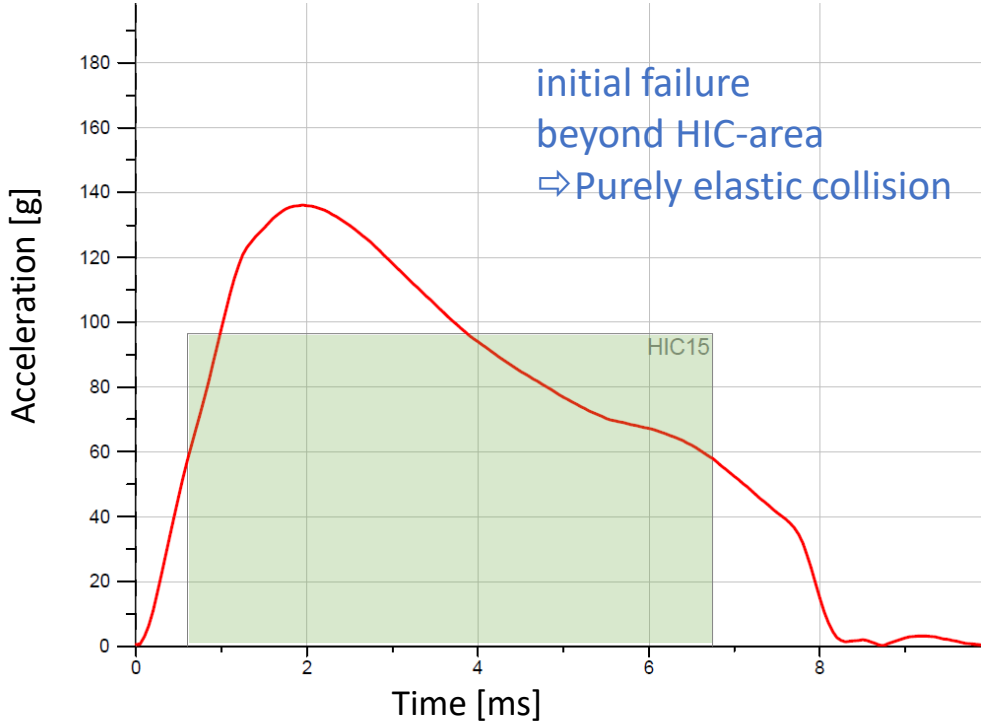
- Head Injury Criterion
- HIC15 = 418 … 566 in 10 identical tests
- Accelerations are completely different

$$\mathrm{HIC} = \max\left\{\left[\frac{1}{t_2-t_1}\int_{t_1}^{t_2} a(t)\mathrm{d}t\right]^{2.5}(t_2-t_1)\right\} < 1000$$





Where does this Scatter come from?

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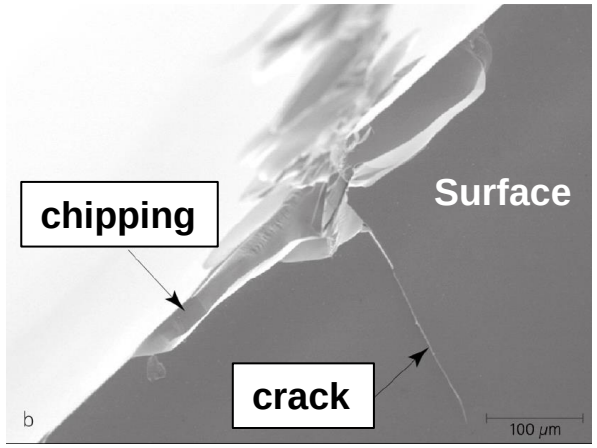
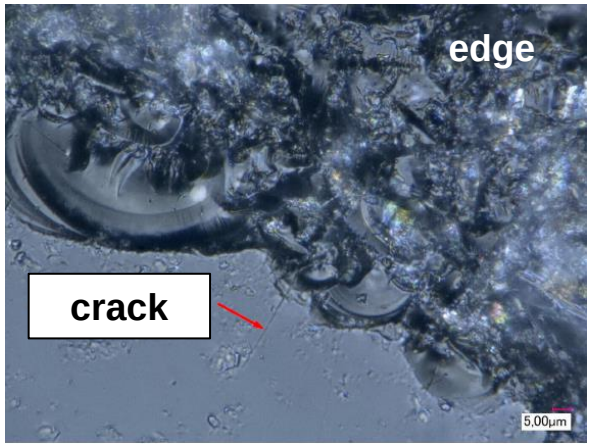
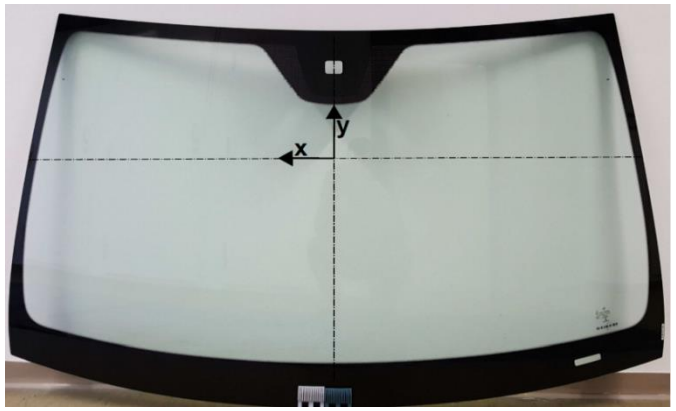
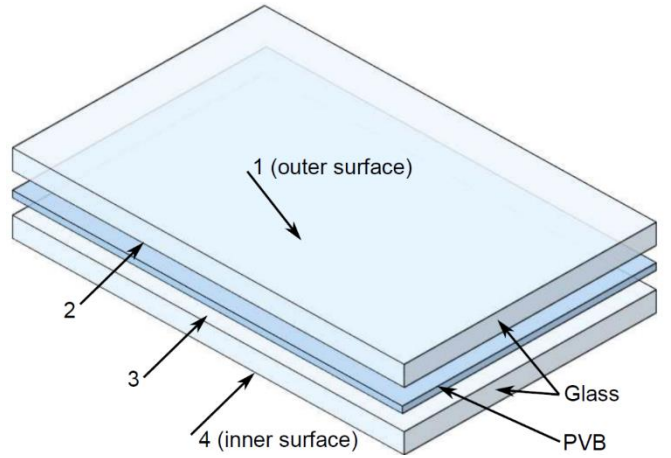
- The reasons are microcracks in the surface / edge of the glass









- These are production and handling related:
  - Edge processing
  - Silkscreen
  - Transportation

- Different stress at failure for all 4 surfaces, edges and screen-printing area must be considered in the simulation

How to determine the probability of fracture?

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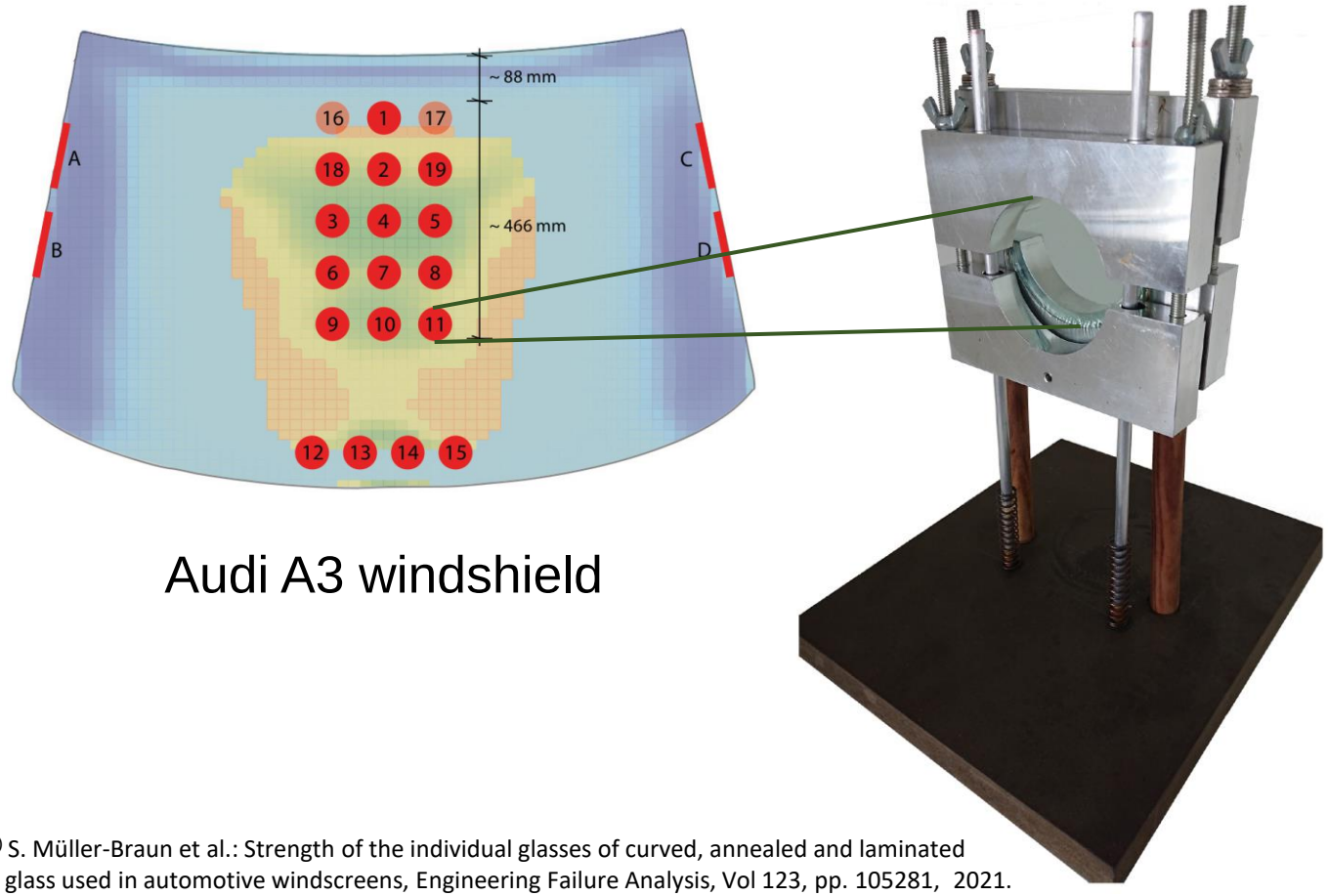
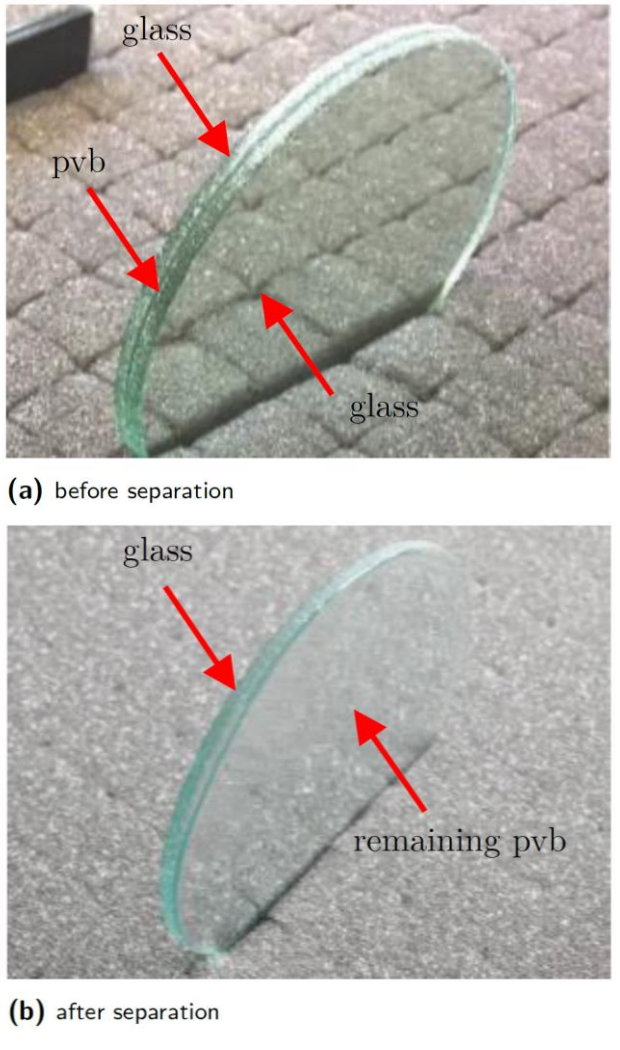
➢ Specimen preparation[1)]



Audi A3 windshield



[1)] S. Müller-Braun et al.: Strength of the individual glasses of curved, annealed and laminated glass used in automotive windscreens, Engineering Failure Analysis, Vol 123, pp. 105281, 2021.

How to Determine the Probability of Fracture?

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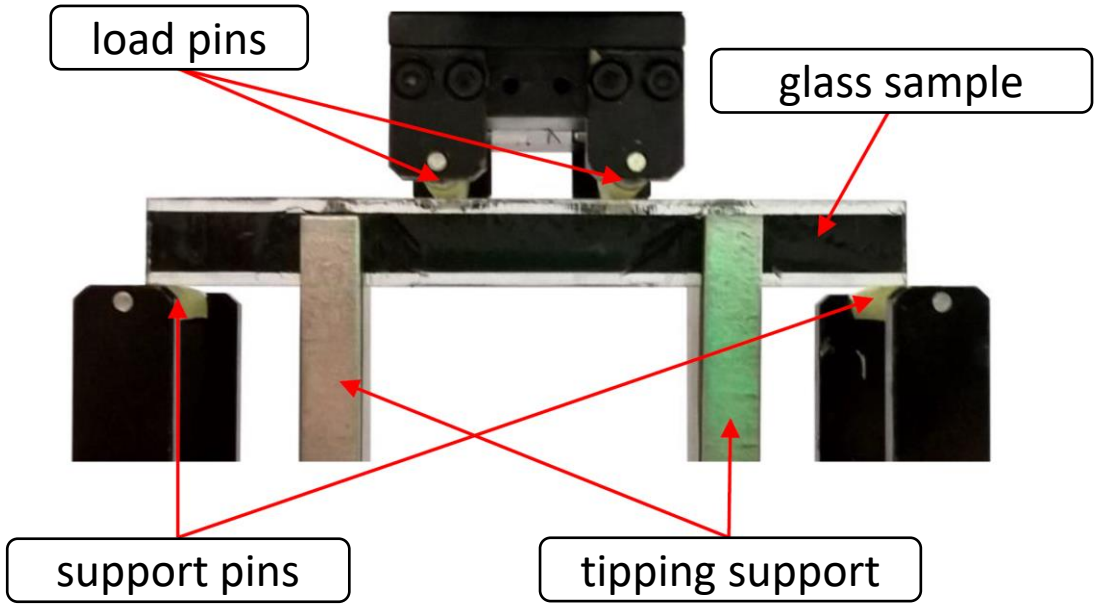
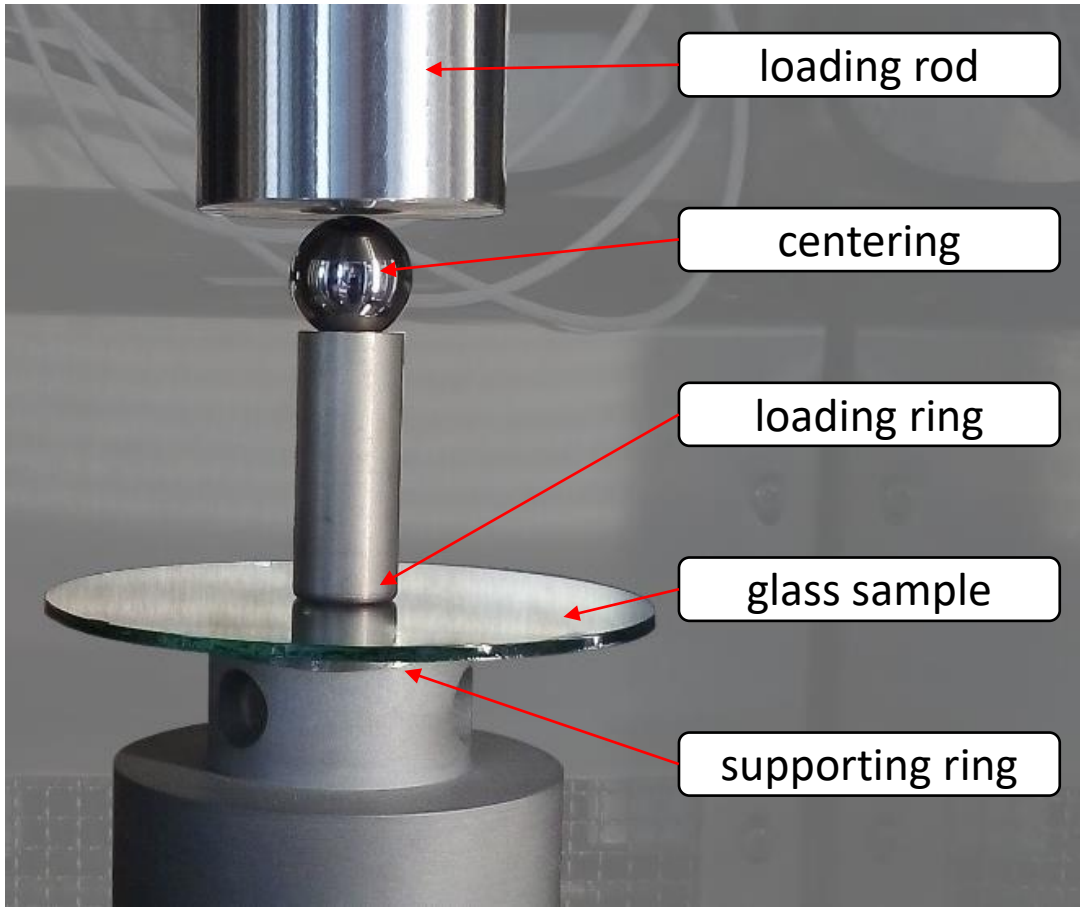
- Small specimens (quasi-static)[1]:
  - waterjet cutting / separation
  - coaxial ring-on-ring tests (surface)
  - four-point bending (edges)





[1] S. Müller-Braun et al.: Strength of the individual glasses of curved, annealed and laminated glass used in automotive windscreens, Engineering Failure Analysis, Vol 123, pp. 105281, 2021.

Probability Distribution – Critical Crack Lengths

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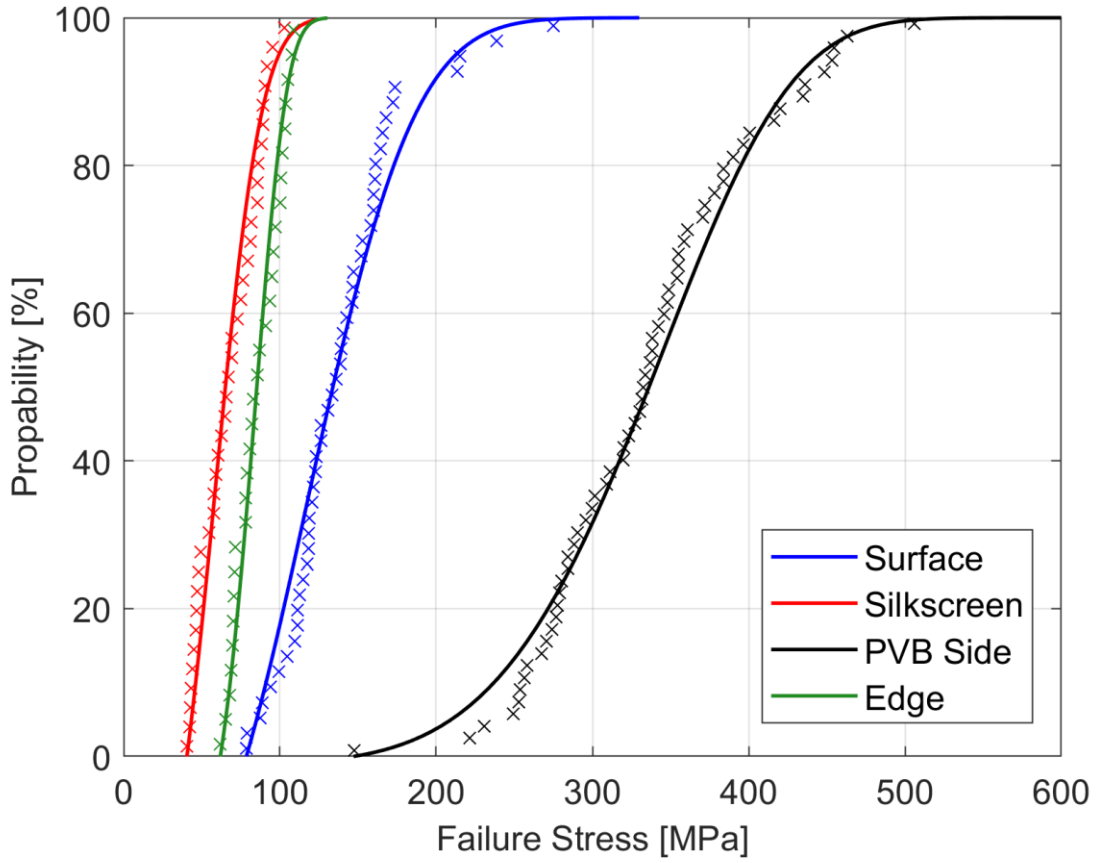
- Statistical evaluation[1)]
- Left truncated Weibull distribution

$$P(x) = 1 - \exp\left[\left(\frac{\tau}{\eta}\right)^{\beta} - \left(\frac{x}{\eta}\right)^{\beta}\right]$$

  - Scale parameter η
  - shape parameter β
  - Truncation point τ
    $\tau = 0$ yields the well-known two-parameter Weibull distribution

- So far, we obtained the critical and not the initial crack lengths from this distributions !



[1)] S. Müller-Braun et al.: Strength of the individual glasses of curved, annealed and laminated glass used in automotive windscreens, Engineering Failure Analysis, Vol 123, pp. 105281, 2021.

How to Determine the Initial Crack Lengths?

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- For subcritical crack growth, the crack velocity can be expressed by the stress intensity

$$K_{\mathrm{I}} = Y\sigma\sqrt{\pi a} \quad \text{and} \quad K_{\mathrm{IC}} = Y\sigma_f\sqrt{\pi a_f} \quad \text{at fracture}$$

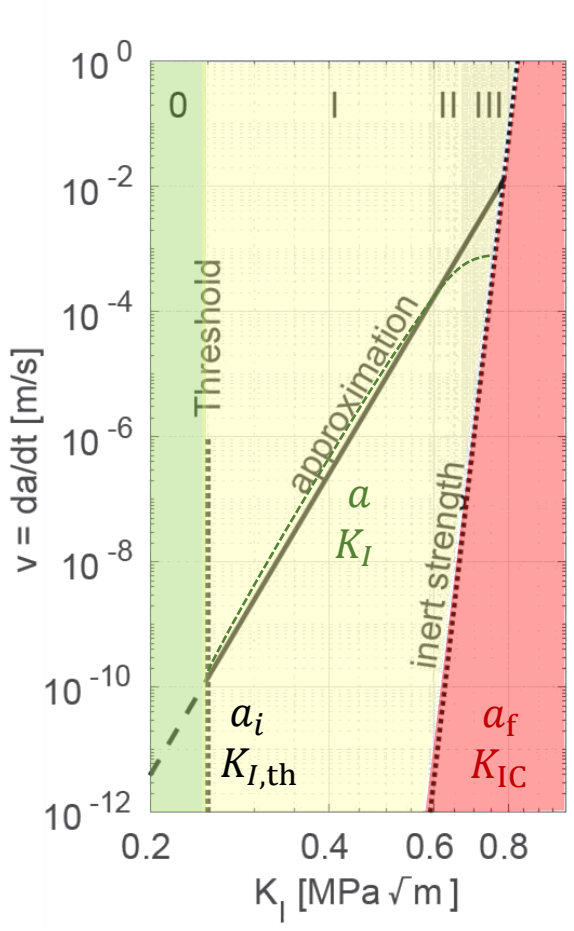
- Linear approximation by parameters n and v_0 yields

$$v = \frac{da}{dt} = v_0 \left(\frac{K_I}{K_{IC}}\right)^n$$

from which the initial crack length a_i can be computed reversely by integration.

- Crack grow parameters[1)]:

H [%rh], 25°C	30	40	50	60	70
n	15.43	15.10	14.75	12.96	12.26
v_0	9.54	10.22	10.47	13.95	15.99



[1)] C. Brokmann et al.: Subcritical crack growth parameters in glass as a function of environmental conditions. Glass Structures & Engineering 6:89–101, 2021.

What About the Rate Dependence of Glass?

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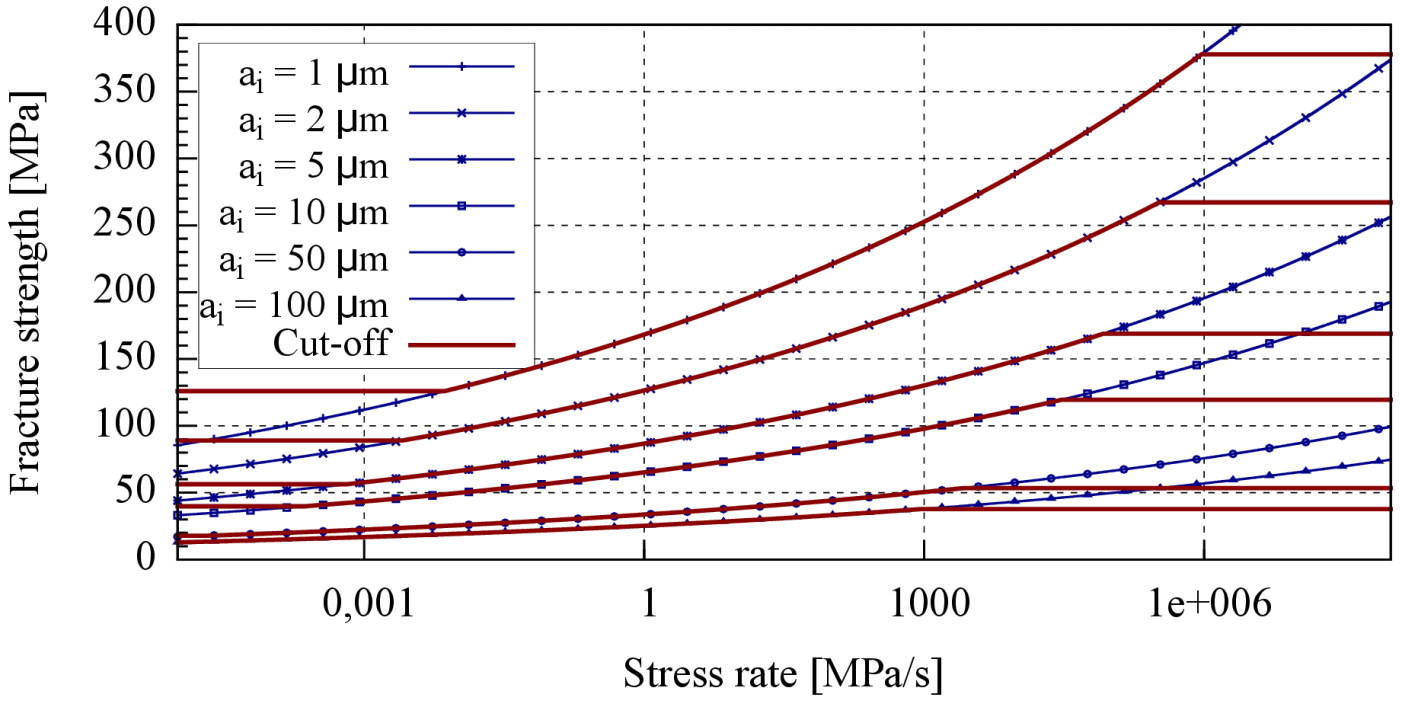
Fracture strength in dependency of the stress rate: $\sigma_{\text{crit.}} = \left(\frac{2(n+1)K_{Ic}^{n}}{v_0 (n-2)\left(Y\sqrt{\pi}\right)^{n} a_i^{\frac{n-2}{2}}} \right)^{1/(1+n)} \dot{\sigma}^{1/(1+n)}$

with $v_0 \approx 6\ \text{mm/s}$ and $n \approx 16$



Lower limit

$K_I = \sigma \sqrt{\pi a}\, Y$

$\sigma_{TH} = \frac{K_{TH}}{\sqrt{\pi a} Y}$

Upper limit

$K_I = \sigma \sqrt{\pi a}\, Y$

$\sigma_{Ic} = \frac{K_{Ic}}{\sqrt{\pi a} Y}$

Non-Local Failure Model for Glass – Regularization

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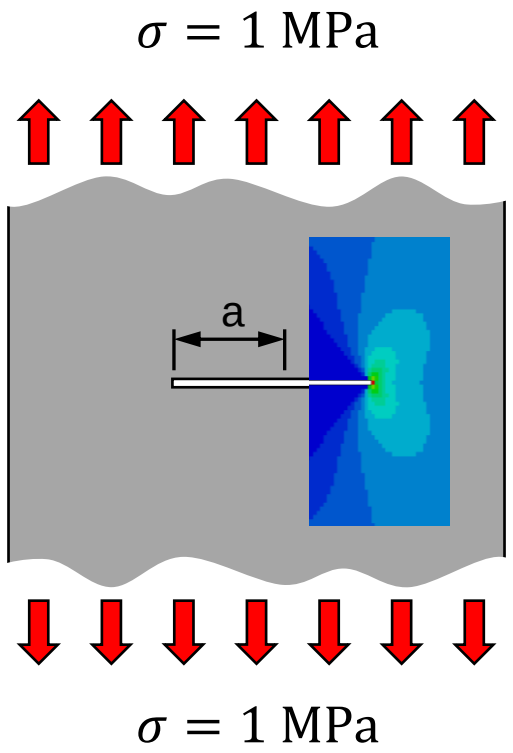
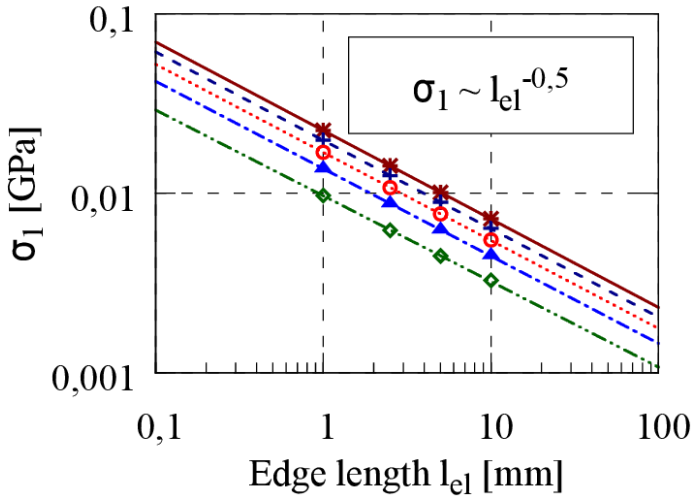
Reduction of strength

- Griffith crack
  - Element size: 10 mm, 5 mm, 2,5 mm, 1 mm
  - Element at the crack tip
- Stress depends on element size
- Stress decreases proportional to $1/\sqrt{l_{el}}$
- Combination of
  - Stress field
  - Element geometry
  - Major stress
- Regularized stress intensity

$$K_I^{\text{Num.}} = \sigma_1 \sqrt{\pi\, l_{el}}\, f_{\text{geo}}$$

$$K_I^{\text{Analyt.}} \sim K_I^{\text{Num.}}$$





Non-Local Failure Model for Glass[1)]

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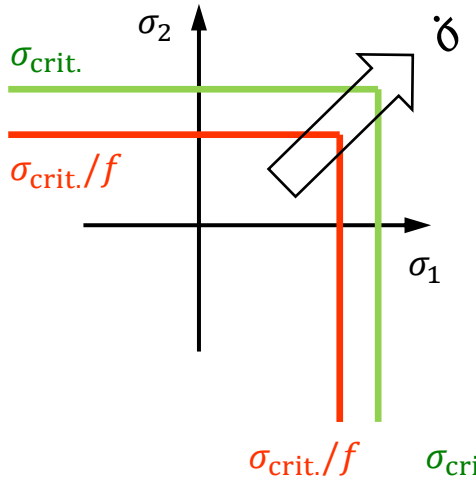
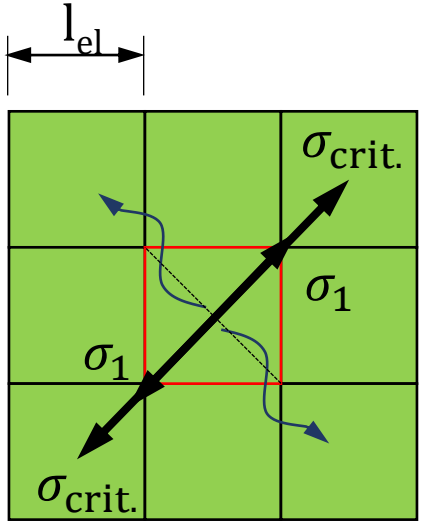
- Major stress criterion
  - $\sigma_{1,2} \geq \sigma_{\text{crit.}}$
- Strength depends on stress rate
  - $\sigma_{1,2} \geq \sigma_{\text{crit.}}\,(\dot{\sigma})$
- Crack orthogonal to principal stress
  - Linear stress reduction
  - $n = \text{int}\left[\frac{l_{el}}{v\,\Delta t}\right]$, v =1,520m/s
- Reduction of strength in crack direction
  - Reduction depends on neighboring fracture state (⇨ non-local)
  - $\sigma_{\text{crit.}} = \begin{cases} \sigma_{\text{crit.}} & \text{without neighboring crack} \\ \sigma_{\text{crit.}}/f(l_{el}) & \text{with neighboring crack} \end{cases}$
- Element erosion after second element perpendicular to first crack failed



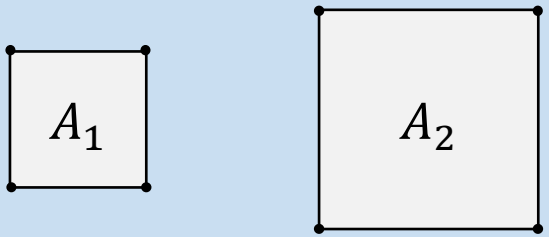


[1)] C. Alter et al. : An enhanced non-local failure criterion for laminated glass under low velocity impact. Int. J. Imp. Eng. 109:342–353, 2017.

Numerical Treatment [1)]

initialization

1. Assign stress at fracture to the Gauss points according to the distribution functions separately for edges, each side of the surface and screen-printing area
2. Regularization of the fracture stress

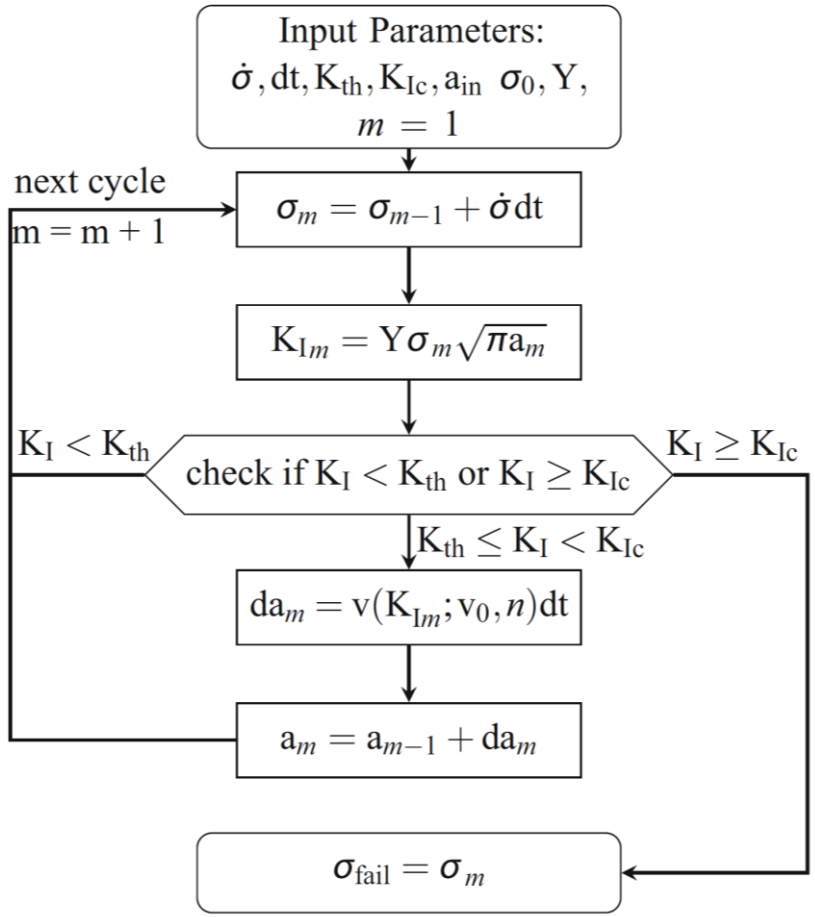


$$\sigma_2 = \sigma_1 \left(\frac{A_1}{A_2}\right)^{-\frac{1}{\beta}}$$

3. Calculate the initial crack length in each Gauss point

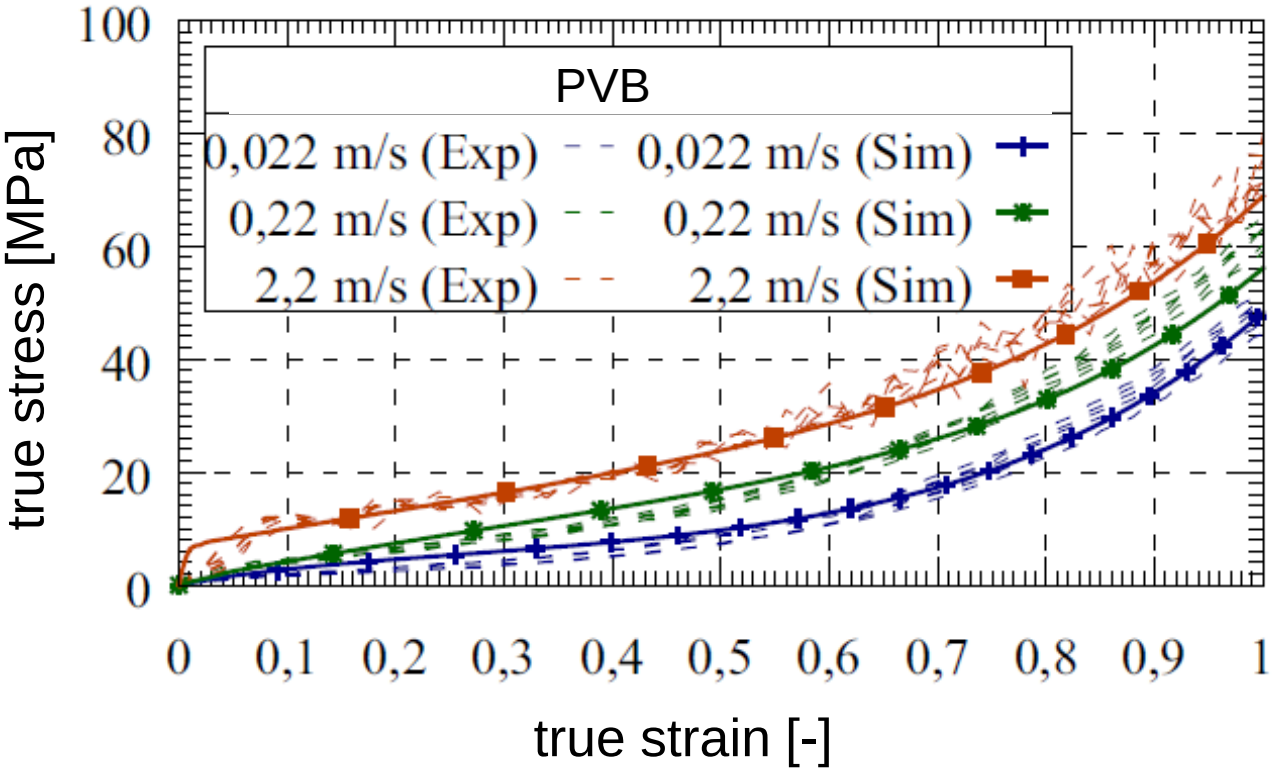
simulation

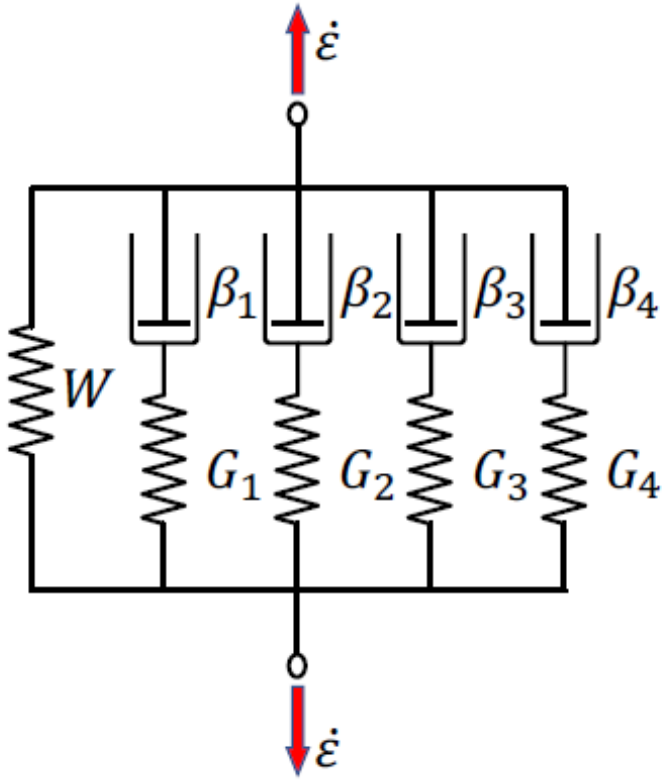
4. Compute subcritical crack growth
5. Activate (non-local) failure criterion



[1)] C. Brokmann et al.: Subcritical crack growth parameters in glass as a function of environmental conditions. Glass Structures & Engineering 6:89–101, 2021.

PVB – Interlayer: ∗MAT_GENERAL_HYPERELASTIC





$$W_{DEV}(I_C, II_C) = \sum_{i,j=0}^{n} A_{ij}(I_C - 3)^i (II_C - 3)^j$$

FE-Model for Laminated Glass

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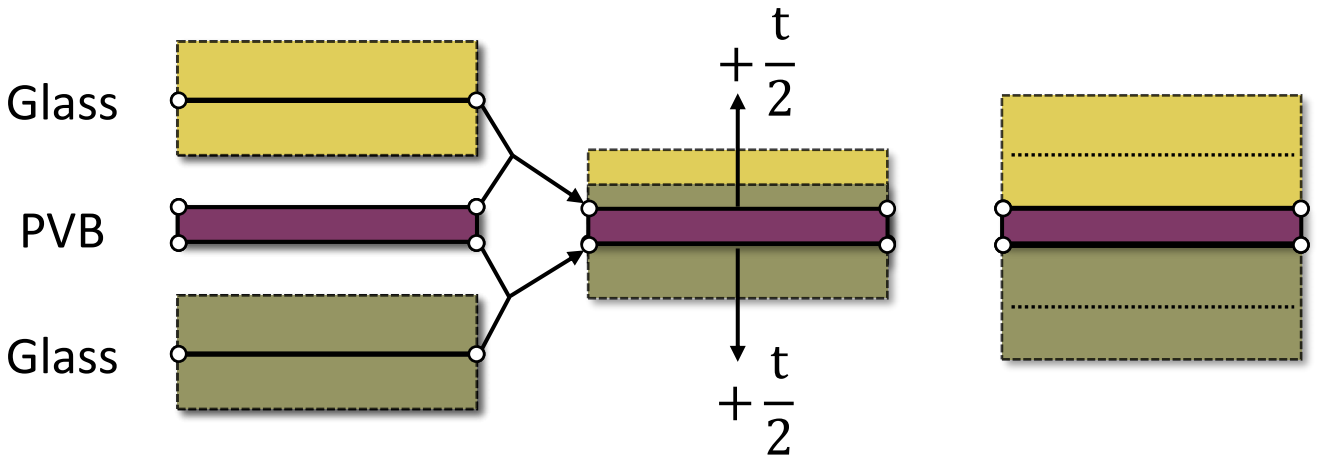
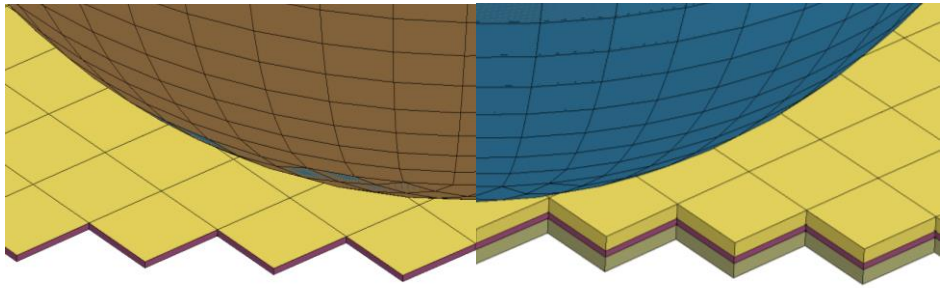
- Element types
  - Glass: Shell elements
    linear elastic
    non-local failure criterion
  - PVB: Solid elements
    hyperelastic
- Coincident coupling
- Shift of shell
  and contact thickness



Visualization of shifted shell thickness



- Regular mesh for the windscreen (2.5 - 10mm)
- Commercial model of the impactor from Lasso
- User subroutines in the explicit
  FE packages Radioss and LS-DYNA

Validation of the Laminated Glass Model

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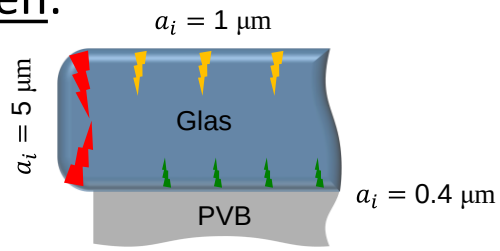
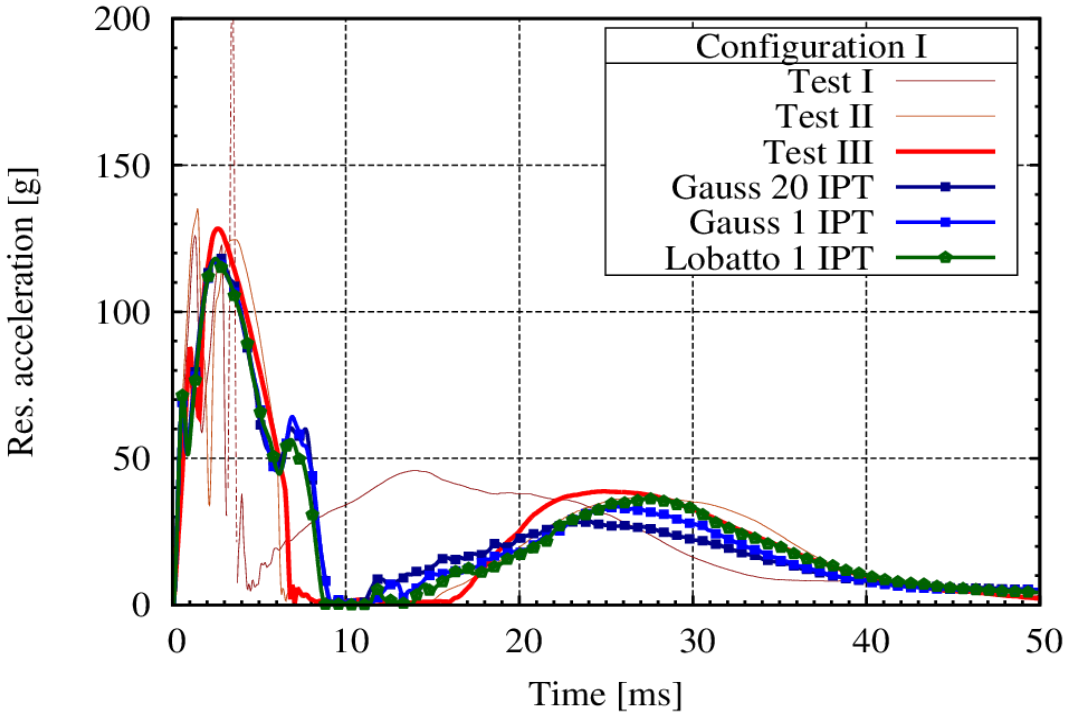
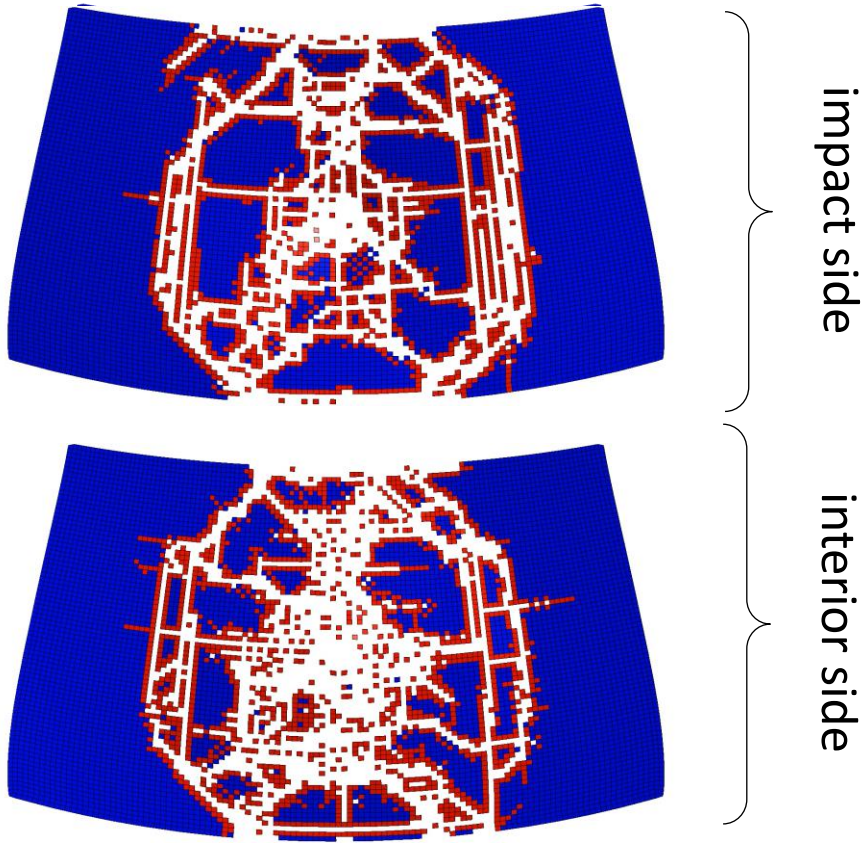
Head impact on center of the windscreen:

- Integration points at the glass surface
- Element erosion if one integration point fulfills the crack criteria







Stochastic Simulation: HIC as a Probability Value

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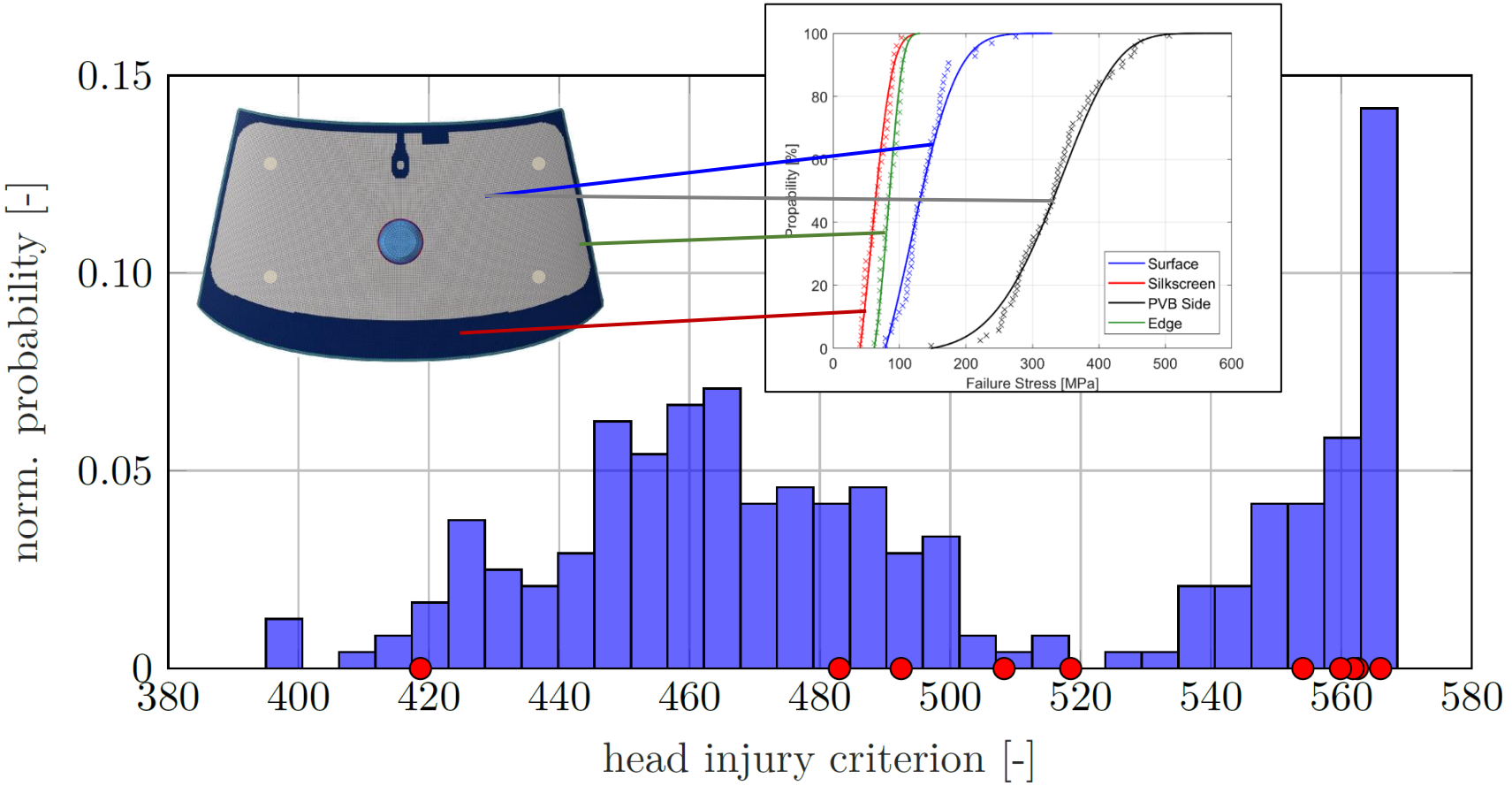
➢ Stochastic simulation, four-point support (250 runs)



Test No.	HIC
1	492
2	483
3	419
4	554
5	562
6	562
7	560
8	566
9	518
10	508

Stochastic Simulation: HIC as a Probability Value

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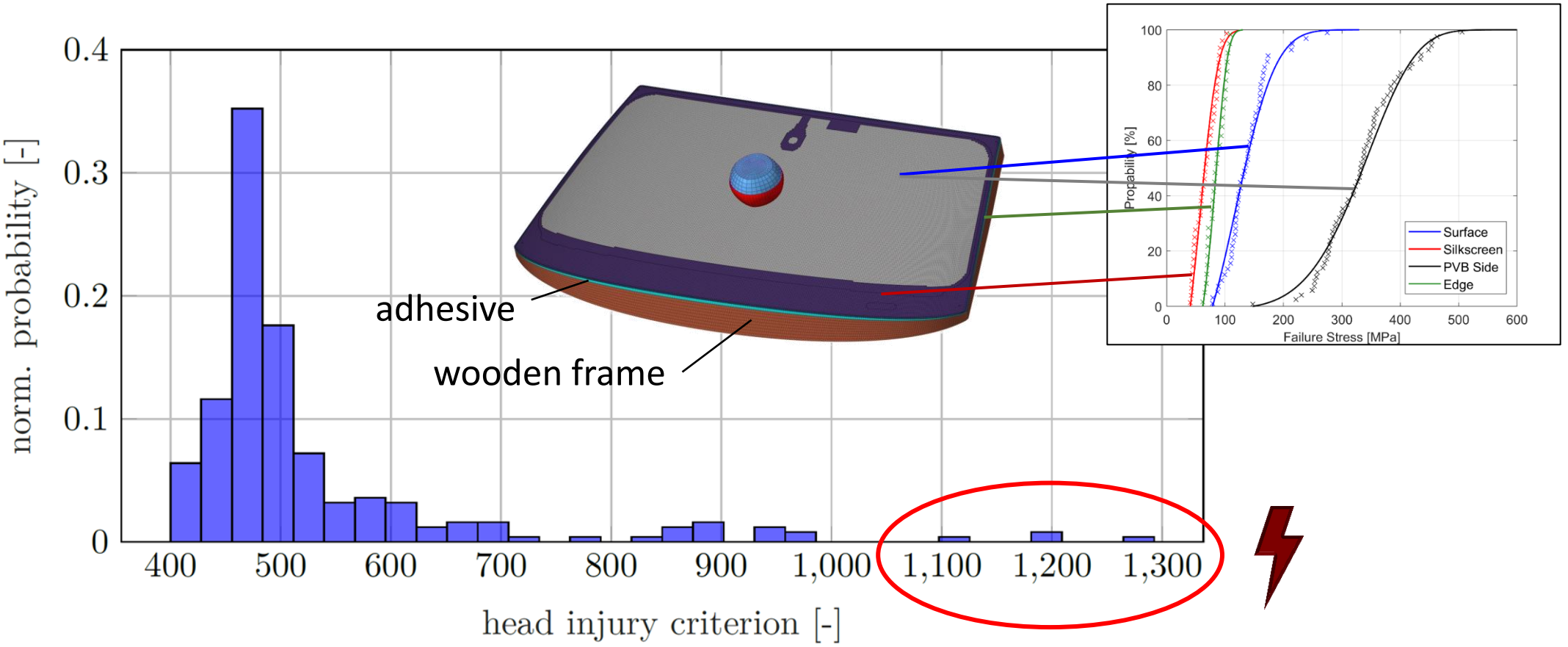
➢ Test setup close to the car and stochastic simulation (250 runs)



Summary: The Methodology in a Nutshell

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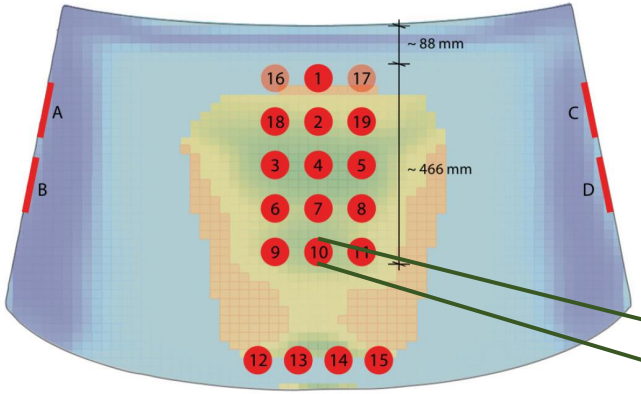
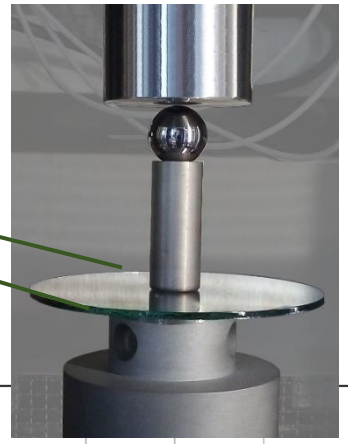
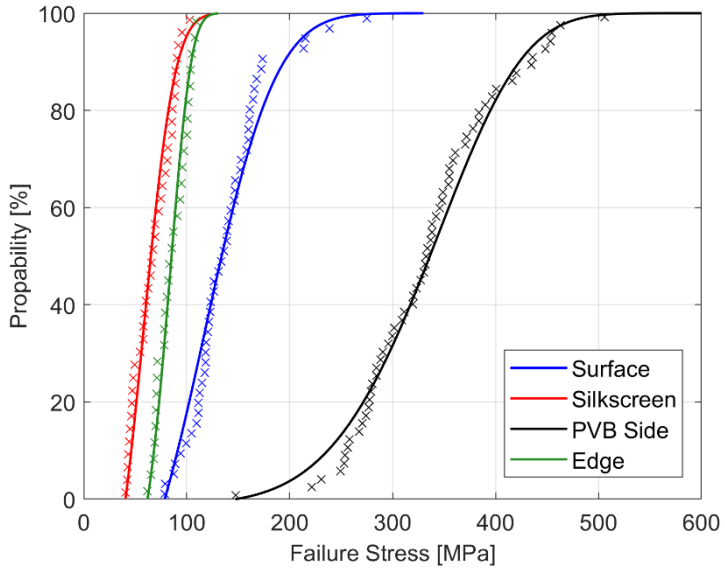


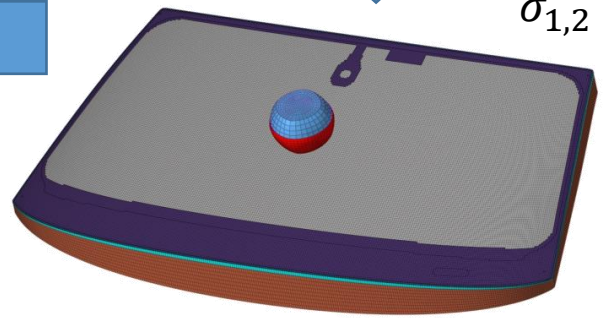


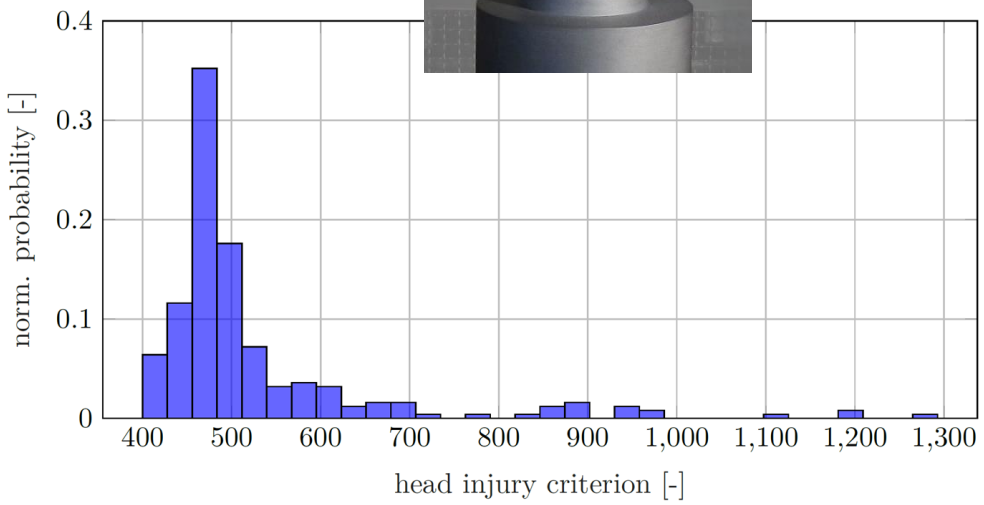
$P(x)$



$$a_i = \int \left(\frac{K_I}{K_{IC}}\right)^n dt$$

$$\sigma_{1,2} \geq \sigma_{\text{krit.}}(\dot{\sigma})$$





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Thank you
for your attention!

Federal Ministry
for Economic Affairs
and Climate Action